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### **Foreword**

In order to improve learning outcomes the Department of Basic Education conducted research to determine the specific areas that learners struggle with in Grade 12 examinations. The research included a trend analysis by subject experts of learner performance over a period of five years as well as learner examination scripts in order to diagnose deficiencies or misconceptions in particular content areas. In addition, expert teachers were interviewed to determine the best practices of ensure mastery of thetopic by learners and improve outcomes in terms of quality and quantity.

The results of the research formed the foundation and guiding principles for the development of the booklets. In each identified subject, key content areas were identified for the development of material that will significantly improve learner's conceptual understanding whilst leading to improved performance in the subject.

The booklets are developed as part of a series of booklets, with each bookletfocussing onlyon one specific challenging topic. The selected content is explained in detail and include relevant concepts from Grades 10 - 12 to ensure conceptual understanding.

The main purpose of these booklets is to assist learners to master the content starting from a basic conceptual level of understanding to the more advanced level. The content in each booklets is presented in an easy to understand manner including the use of mind maps, summaries and exercises to support understanding and conceptual progression. These booklets should ideally be used as part of a focussed revision or enrichment program by learners after the topics have been taught in class. The booklets encourage learners to take ownership of their own learning and focus on developing and mastery critical content and skills such as reading and higher order thinking skills.

Teachers are also encouraged to infuse the content into existing lesson preparation to ensure indepth curriculum coverage of a particular topic. Due to the nature of the booklets covering only one topic, teachers are encouraged to ensure learners access to the booklets in either print or digital form if a particular topic is taught.

### 2. How to use this booklet

### Purpose

To a large extent, the National Diagnostic Reports highlightcommon problems that learners experience when answering National Examination question papers.

Among other things, these reports highlight the following problems:

- · "One of the major problems inboth papers is learners' poor command of the relevant terminology and definitions."
- · "Learnersdid not know abbreviations."
- · "Candidates did not complete the entire table."
- "Candidates did not use the given formula."
- · "Candidates struggled to covert Botswana pula into South African rand."

In answering Mathematical Literacy questions, you should always make use of the information given. This information is often given as the context within which the problem must be solved. The purpose of this booklet is therefore to help you to extract such information from a given context in Mathematical Literacy examinations as well aswhen doing the exercises found in textbooks.

Mathematical Literacy is taught and tested in a real-life authentic context. In order to sketch this context, a variety of texts, tables, pictures, diagrams, annexures, etc. are used. It follows that one of the skills needed to solve Mathematical Literacy problems is extracting the 'knowns' and the 'unknowns' from the given context.

'Knowns' are defined as information given in the context of a question, and 'unknowns' are defined as information given within a question.

Each section starts with examples, followed by fully calculated answers and explanations.

Activities based on the examples follow, to allow you to practise the skills you have acquired after reading the example.

The answers to all the activities are in **Section6: Check Your Answers**.

### 1.Examination tipsfor Mathematical Literacy

### 3.1Paper 1(set in a familiar context)

- 5 Questions
  - Question 1
    - ■30 marks (±5)
    - Level 1 type questions only
    - •All 5 application topics
  - Question 2
    - Finance
    - ■Level 1 to 3 type questions
  - Question 3
    - Measurement
    - ■Level 1 to 3 type questions
  - Question 4
    - •Maps, plans and other representations from the real world
    - ■Level 1 to 3 type questions
  - Question 5
    - Data handling
    - ■Level 1 to 3 type questions
- Mark allocation per topic in Mathematical Literacy P1
  - Finance (± 52 marks)
  - Measurement (± 30 marks)
  - o Maps, plans and other...from the real world (± 23 marks)
  - Data handling (± 37 marks)
  - Probability (minimum 8 marks)
- Cognitive levels for Mathematical Literacy P1

All levels have a range of ±5%

- Level 1: 90 marks (60% of P1)
- Level 2: 53 marks (35% of P1)
- Level 3: 7 marks(5% of P1)
- Level 4: 0 marks (0% of P1)

### 3.2Paper 2(set in a familiar and an unfamiliar context)

### • 4 OR 5 Questions

- Question 1
  - Integrated application topics
  - Level 2 to 4 type questions
- o Question 2
  - Integrated application topics
  - Level 2 to 4 type questions
- Question 3
  - Integrated application topics Level 2 to 4 type questions
- Question 4
  - Integrated application topics
  - Level 2 to 4 type questions

### AND / OR

- Question 5
  - Integrated application topics
  - Level 2 to 4 type questions

### Mark allocation per topic in Mathematical Literacy P2

- Finance (± 52 marks)
- Measurement (± 30 marks)
- Maps, plans and other...from the real world (± 23 marks)
- Data handling (± 37 marks)
- Probability (minimum 8 marks)

### Cognitive levels for Mathematical Literacy P2

All levels have a range of ±5%

- Level 1:0 marks (0% of P2)
- Level 2:37 marks (25% of P2)
- Level 3:53 marks (35% of P2)
- Level 4: 60 marks (40% of P2)

### 3.3 Allocation of examination marks (i.e. Paper 1 and Paper 2 combined)

Cognitive Levels:

Level 1: 90 marks or 30% for P1 and P2 combined.

Level 2: 90 marks or 30% for P1 and P2 combined.

Level 3: 60 marks or 20% for P1 and P2 combined. Level 4: 60 marks or 20% for P1 and P2 combined.

### 3.4 Key features of a Mathematical LiteracyPaper 1examination

Paper 1 is the easierquestion paper of the two, for the following reasons:

- 90 of the 150 marks are allocated to Level 1 type questions.
- It is set in a familiar context.
- Question 1(30 marks ±5) contains Level 1 type questions only with a short description of the context.

You will be able to scorethese marks if you workthrough past examination papers, work in the classroom everyday, and complete all tasks given by the educator.

Examples of these Level 1 type questions are listed in the following past DBE examination papers:

2017 June examination P1

2017 November examination P1

2018 March examination P1

2018 June examination P1

### 3.5 Time management for examination preparation

If you have 100 hours to prepare for the examination, the following can be used as a guide regarding how to use your hours:

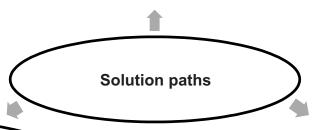
Application topics	Number of hours		
Finance	35		
Measurement	20		
Maps, plans and other	15		
Data handling	25		
Probability	5		

### 1. Overview

Solution pathways (carrying out the steps from 'known' to 'unknown')

### Read from a source

- Graph/ table/ formula/ map/ plans/ diagrams, etc.
- Identify the unknown and write down the answer.



# Use the given formula/ formulae to relate the known to the unknown

- Identify the knowns and unknowns in the given formula.
- Ensure that similar quantities are expressed in the same unit of measurement.
- Ensure that the quantities of the known are expressed in the same unit as that of the unknown.
- Substitute the known quantities correctly.
- Perform the necessary calculations correctly; then write down the answer, i.e.the unknown.

# To perform a simple mathematical calculation

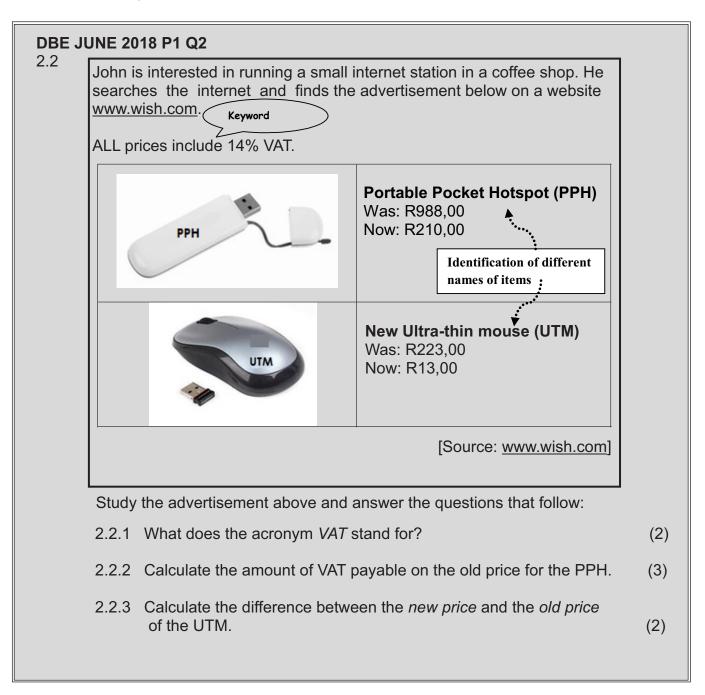
- Calculate the unknown from the given information.
- Identify or recall a mathematical relationship between the known and the unknown and write it down.
- Perform the calculations and obtain the unknown.

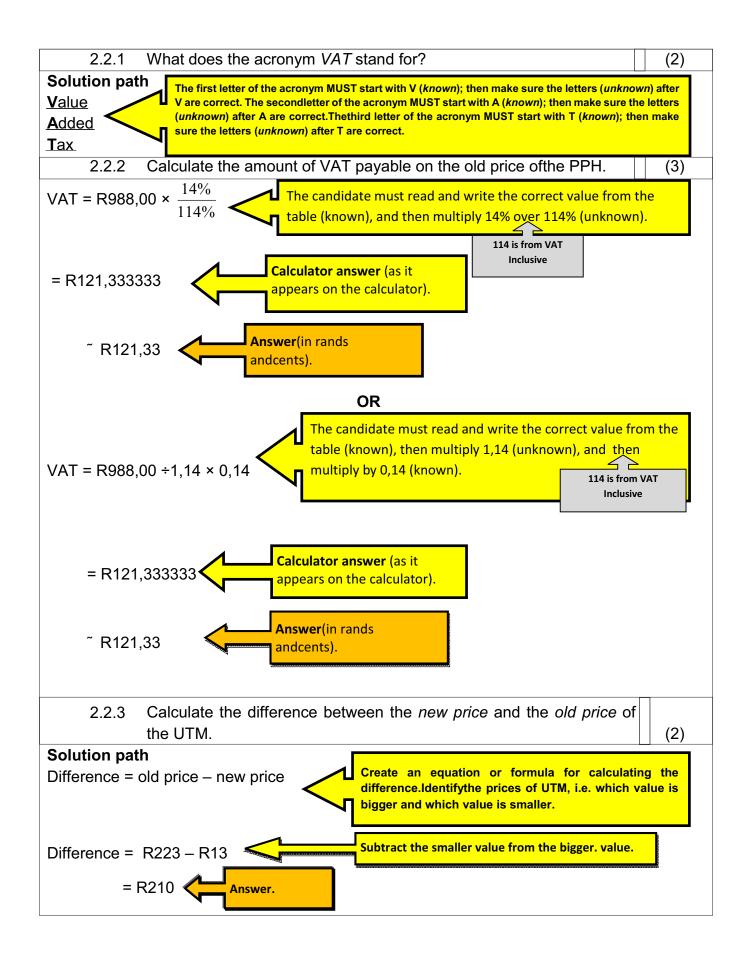
### 1. Solution paths

### Example 2

Identify the following from the text below:

- 1. Knowns
- 2. Unknowns
- 3. The relationship between the known and the unknown.





### **Activity 1**

### Α

Identify the following from each of the questions below:

- 1. Knowns
- 2. Unknowns
- 3. The relationship between the known and the unknown
- Tyrone buys chocolates in bulk to make gift baskets containing different chocolate bars, which he will sell. He buys boxes that contain bars of Peppermint Crisp, BarOne, Kit Kat, and Cadbury 80g chocolate slabs.

  Picture of a gift basket with chocolate bars.

Determine the total price of a box of Peppermint Crisp bars if there are 1.1.1 40 bars in a box and the unit price of a bar is R8,70. (2)Solution path Multiply the price of a bar with number of bars in a box. **Answer** 1.1.2 Explain the term profit. (2)Solution path Identification of 3 key words. Construct/ form a sentence. A box of Kit Kat bars costs R435,04. To determine the selling price, 1.1.3 Tyrone increases the cost price by 40%. Determine the amount that he adds to the cost price. (2)Solution path Multiply the percentage increase by the price of a box of Kit Kat bars. Calculator answer (as it appears on the calculator). Answer(in rands andcents).

DBE JUNE 2017 P1 Q1

### **DBE NOV 2017 P1 Q2**

2.3 Rajesh exchanged a gift of £360,00 into South African rand at a bank.

The exchange rate was R1,00 = £0,05773.

The bank charged 1,95% commission on the amount exchanged.

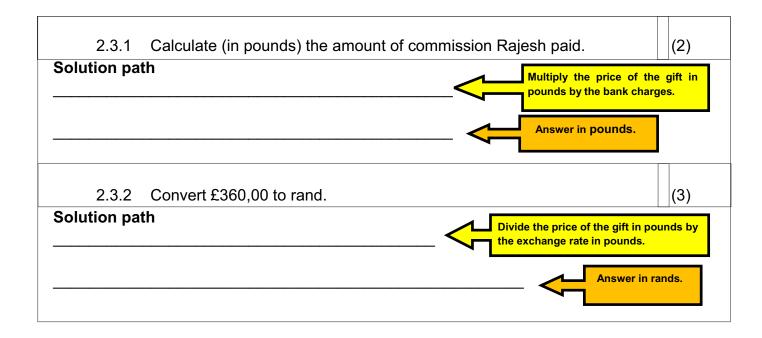
Rajesh then invested R5 000 of his gift in a fixed deposit account for  $1\frac{1}{2}$  years at a compound interest rate of 6,3% per annum.

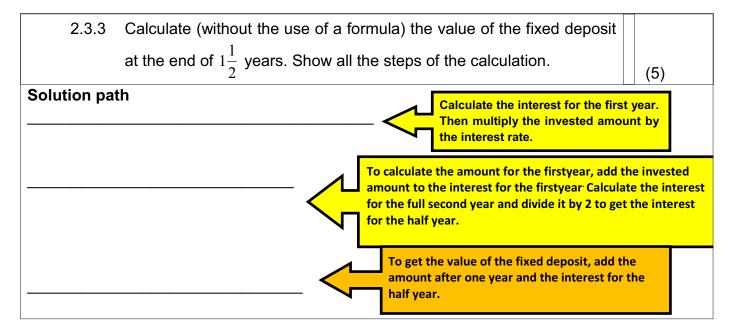
- 2.3.1 Calculate (in pounds) the amount of commission Rajesh paid.
- 2.3.2 Convert £360,00 to rand. (3)

(5)

2.3.3 Calculate (without the use of a formula) the value of the fixed deposit

at the end of years. Show all the steps of the calculation.





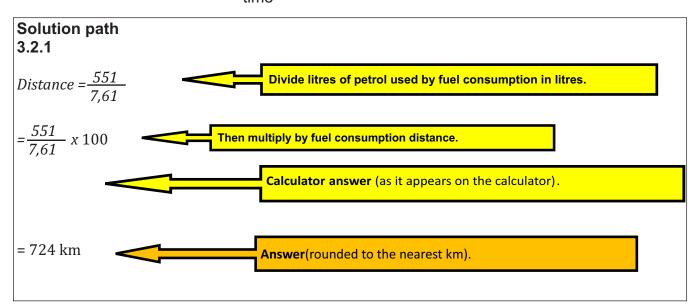
C

### **DBE MARCH 2018 P1 Q3**

- 3.2 A nurse uses a sedan vehicle to travel. The fuel consumption of her vehicle is 7,6 litres per 100 km when travelling at an average speed.
  - 3.2.1 Calculate (to the nearest km) the distance her vehicle can travel using 55 litres of petrol. (3)
  - 3.2.2 The nurse spends 1 hour and 45 minutes on a particular day driving between two workstations that are 189 km apart. Determine the average speed of the vehicle.

Use the following formula:

Average speed = distance time (3)



# Solution path 3.2.2 $Time = \frac{551}{7,61} = 0,75$ Convert known given time into hours, i.e. 45 min into hours. Total Time = 1+0,75 = 1,75 Then add the answer to 1 hour. Average $speed = \frac{189}{1,75}$ Substitute the formula. = $108 \ km/h$ Answer in units.

# DBE JUNE 2018 Q5 QUESTION 5

5.1 Statistics South Africa (STATSSA) collects and releases data based on passenger transport annually. TABLE 2 below shows the 2016 data for land passenger transportation

TABLE 2: 2016 DATA FOR LAND PASSENGER TRANSPORT K

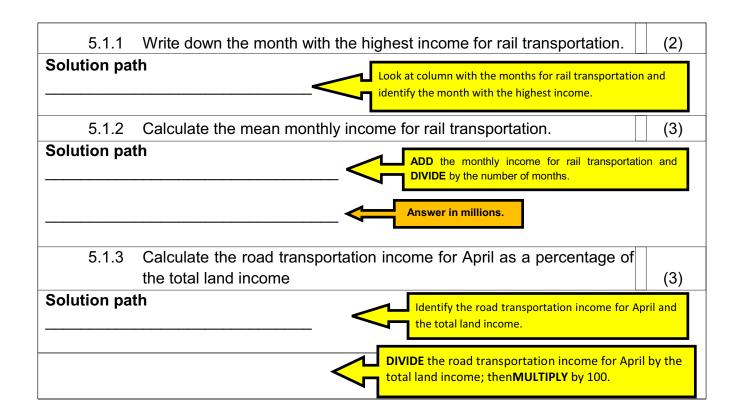
	LAND TRANSPORT				TOTALLAND	
	RAIL		ROAD		TOTAL LAND	
	Passenger journeys in thousands	Income in millions (R)	Passenger journeys in thousands	Income in millions (R)	Passenger journeys in thousands	Income in millions (R)
JAN.	30 526	238	24 279	748	54 805	986
FEB.	36 528	266	27 684	757	64 212	1 023
MAR.	34 250	254	30 277	869	64 527	1 123
APR.	32 940	238	24 268	743	57 208	981
MAY	32 372	233	25 940	770	58 312	1 003
JUN.	32 741	216	25 308	790	58 049	1 006
JUL.	31 792	247	23 609	768	55 401	1 015
AUG.	33 550	251	24 835	769	58 385	1 020
SEP.	38 024	275	27 144	836	65 168	1 111
ост.	35 802	269	24 304	771	60 106	1 040
NOV.	34 700	254	25 225	782	59 925	1 036
DEC.	23 592	198	22 313	801	45 905	999
TOTAL	396 817	•••	305 186	9 404	702 003	12 343

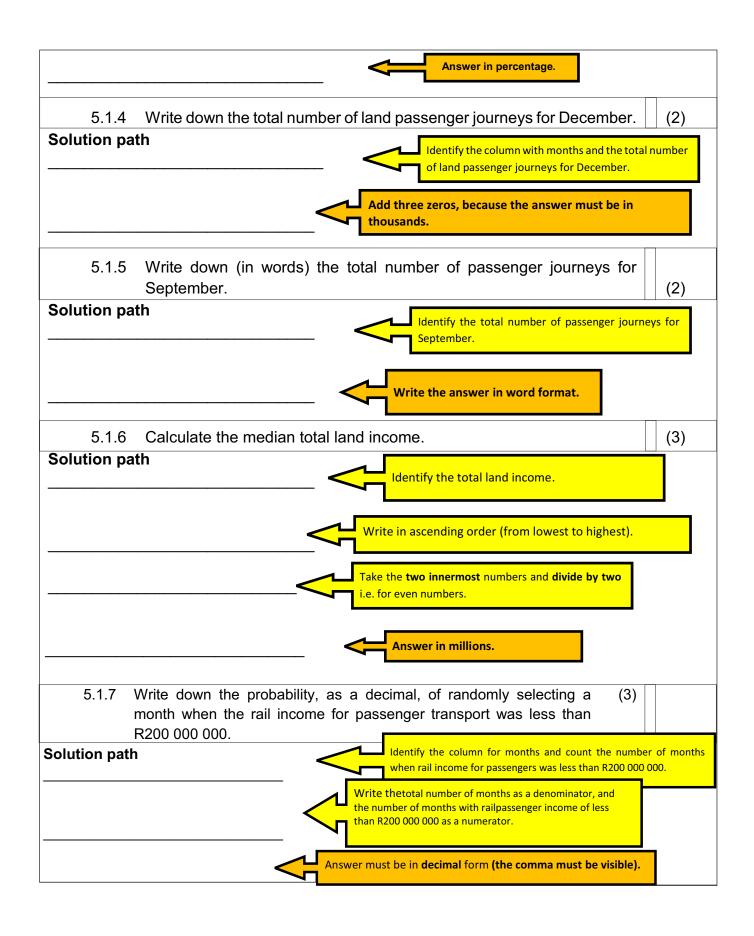
[Adapted from www.statssa.co.za]

Use the table above to answer the questions that follow:

- 5.1.1 Write down the month with the highest income for rail transportation. (2)
- 5.1.2 Calculate the mean monthly income for rail transportation. (3)
- 5.1.3 Calculate the road transportation income for April as a percentage of total land income. (3)
- 5.1.4 Write down the total number of land passenger journeys for December. (2)
- 5.1.5 Write down (in words) the total number of passenger journeys for September. (2)
- 5.1.6 Calculate the median total land income. (3)
- 5.1.7 Write down the probability, as a decimal, of randomly selecting a month when the rail income for passenger transport was less than R200 000 000. (3)
- 5.1.8 A bar graph showing the monthly income for road transport for the last six months of the year, has beendrawn on ANSWER SHEET 1.

On the same set of axes, draw another bar graph that represents the monthly income for rail transport for the last six months of the year. (6)





5.1.8 A bar graph showing the monthly income for road transport for the last six months of the year, has beendrawn on ANSWER SHEET 1.

On the same set of axes, draw another bar graph that represents the monthly income for rail transport for the last six months of the year.

(6)

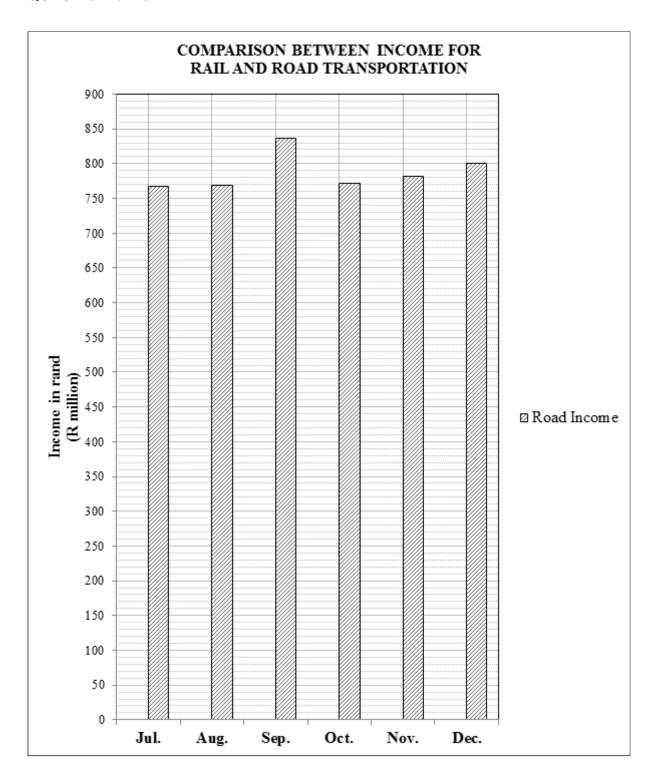
Solution path

Identify the monthly income for rail transport for the last six months of the year, i.e. from July to December).

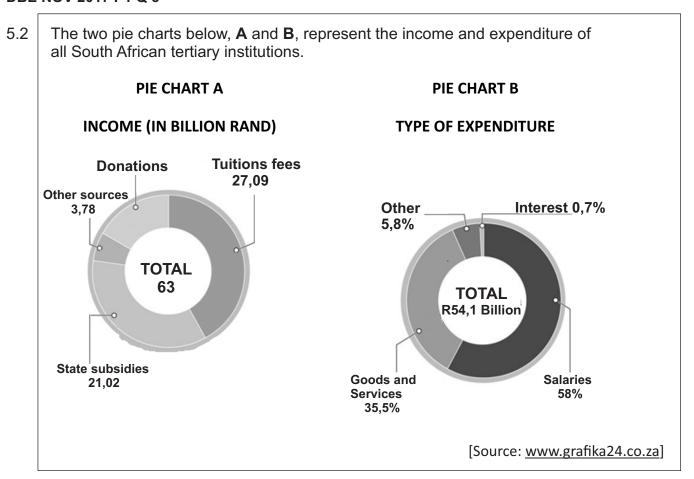
Draw the bar graphs in the correct months, and make sure the height of each bar graph is in the correct position in terms of rand.

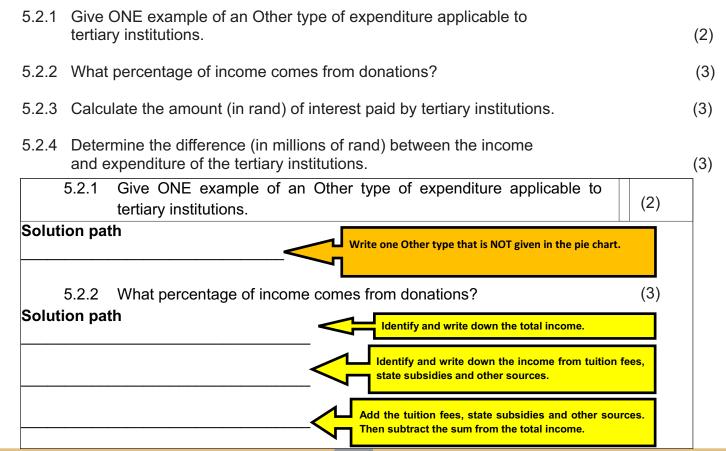
### **ANSWER SHEET 1**

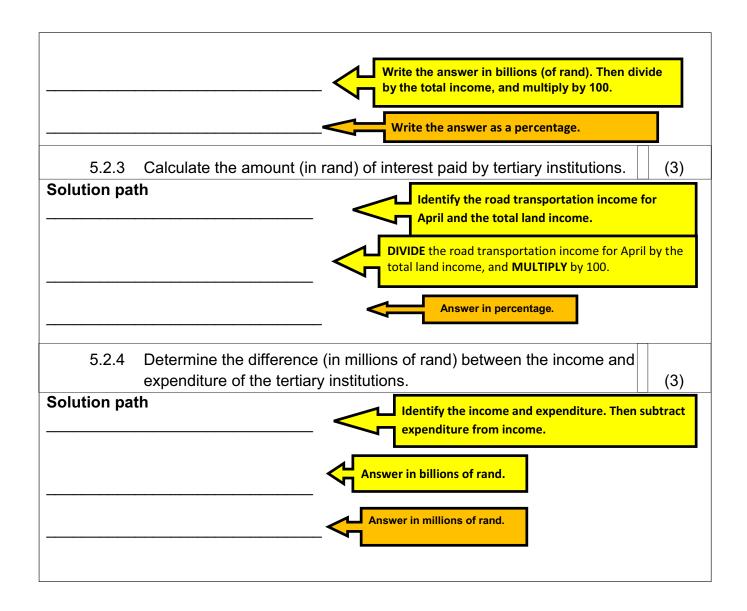
### **QUESTION 5.1.8**



### **DBE NOV 2017 P1 Q 5**







### Understanding the solution path – maps and plans

The solution path consists of the steps completed to get the answer from the given information; that is, executing the steps involved in moving from the 'known' to the 'unknown'.

The examples below illustrate the process.

### Example 1

- **1.**Rammone plans to travel from Colesberg to Port Elizabeth using only national roads.
- Diagram 1 alongside shows a strip chart of the route from Colesberg to Port Elizabeth. Use Diagram 1 to answer the questions that follow.
- 1.1 Name the national roads that Rammone will use to travel to Port Elizabeth.
- 1.2 Which national park is furthest from the N10?
- 1.3 Rammone met a friend in Paterson who had to travel 61km via the R336 from his hometown. Name the friend's hometown.
- 1.4 Write down the names of the two national parks shown on the map.
- 1.5 Calculate the travel distance between the TWO national parks.

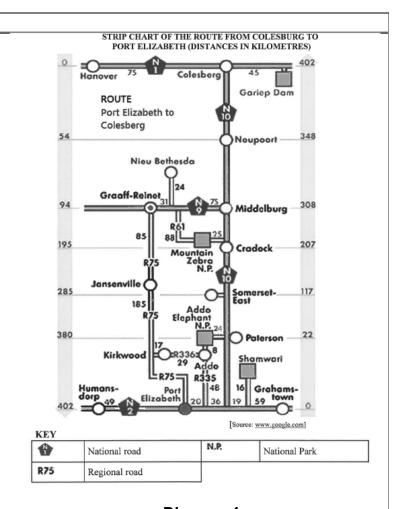
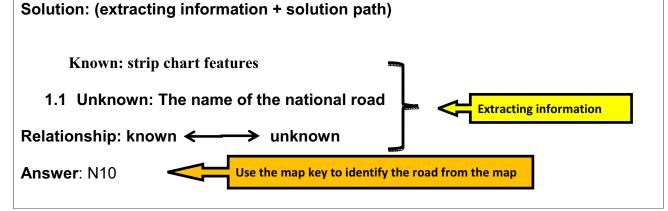
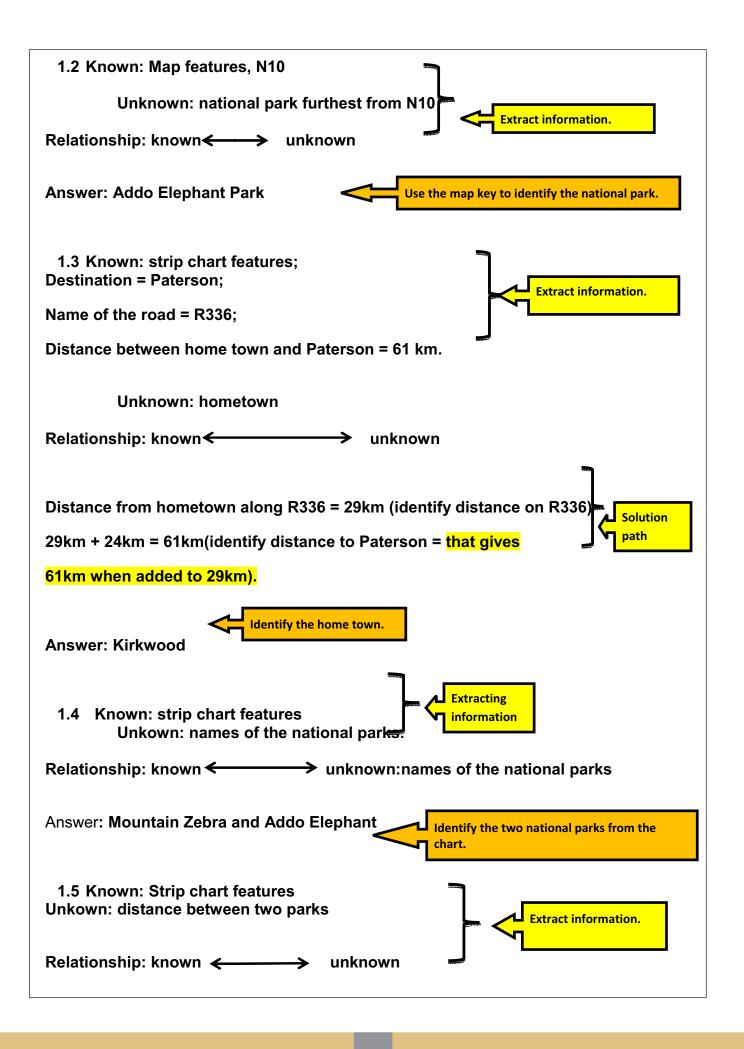


Diagram 1





Distance from Mountain Zebra to Cradock = 25km (identify the distance onthe chart).

Distance from Cradock to Paterson = 185km (calculate the distance onthe chart).

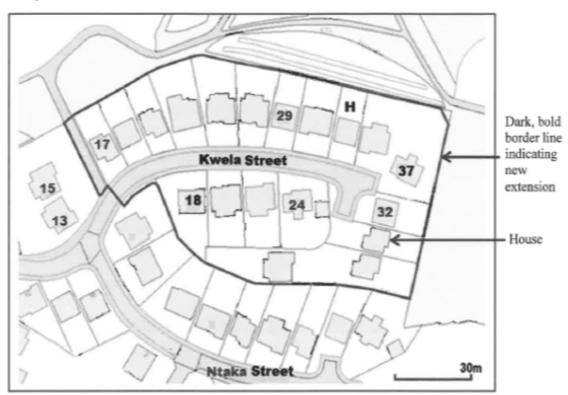
Distance from Paterson to Addo Elephant = 24km (identify the distance onthe chart).

Solution path

### **ACTIVITIES**

Activity A (In this activity, work out a complete solution to the question. DO NOT write the steps you take in words. Simply show them by doing the necessary calculations.)

### Map of Mandela Park Extension



Enlargement of a section of the main map

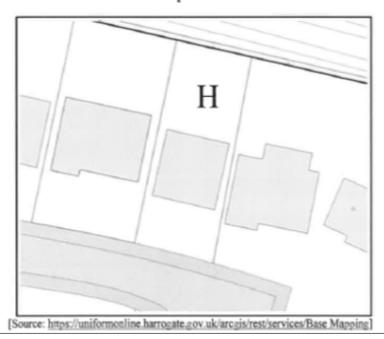
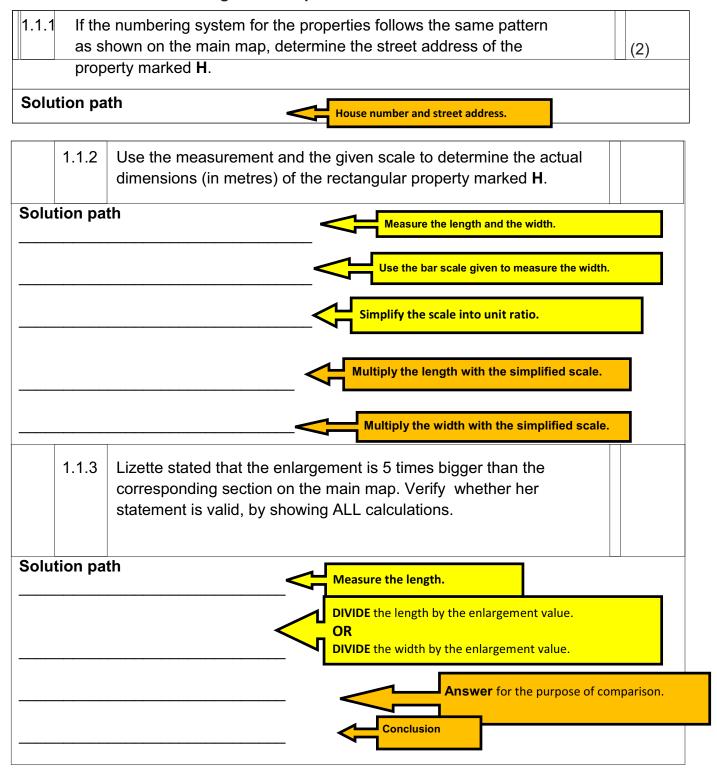
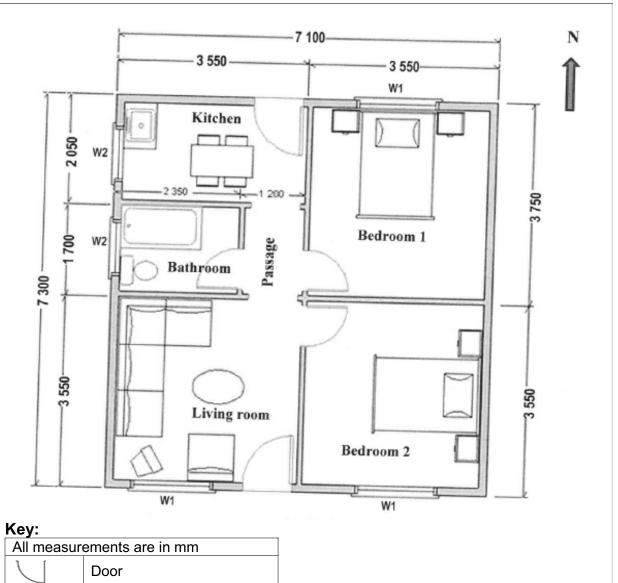


Diagram 2: Map of Mandela Park

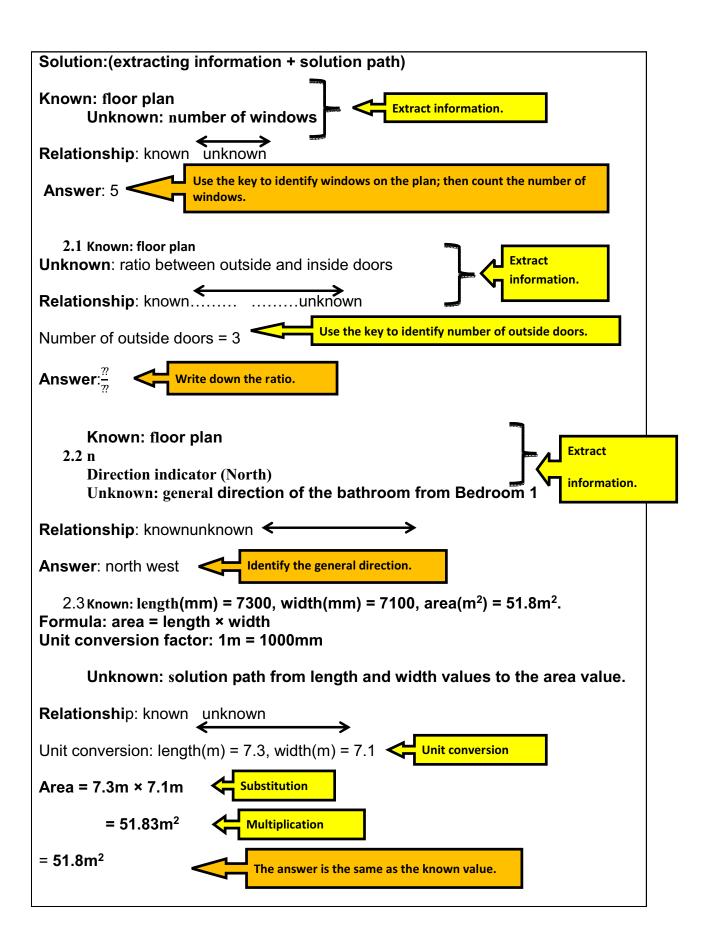




All measurements are in mm				
$\bigcup$	Door			
	Window			

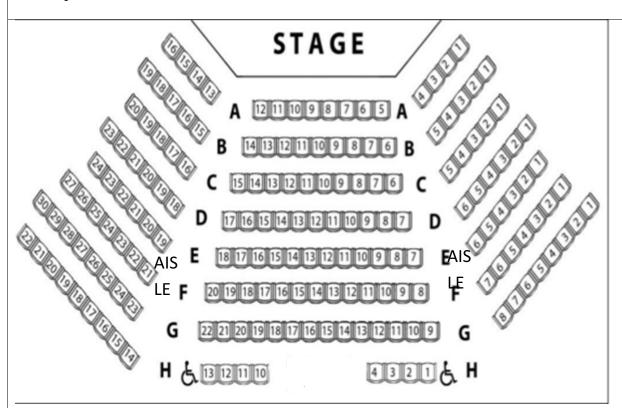
- 2. Diagram3 above shows the floor plan of an RDP house. Use the floor plan to answer the following questions.
- 2.1 Determine the total number of windows shown on the plan.
- 2.2 Write down the ratio (in simplified form) of the number of outside doors to the number of inside doors.
- 2.3 Write down the general direction of the bathroom from Bedroom2.
- 2.4 Show, with calculations, how the total living area of 51.8 m<sup>2</sup> was determined. The following information should be used:

Area = length × width 1m = 1000mm



### **ACTIVITIES**

### **Activity B:**



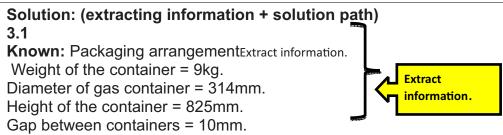
**Diagram 4: Baxter Theatre, Cape Town** 

- **2. Diagram 4** above shows theseating plan in the Baxter Theatre in Cape Town. Use Diagram 4 to answer the questions that follow. Indicate only the known, the unknown and the relationship between them in each question.
  - 2.1 Determine the total number of chairs in the cinema.
  - 2.2Thembi bought a ticket to attend a concert at the Baxter Theatre. Determine the probability that Thembi gets a ticket for a seat in row G.
  - 2.3 Thembi gets a ticket for G5. She wants to go and say hello to her friend who is sitting at seat A13. Use the words *left, right, up*and*down*to give directions for the shortest route Thembi should take.
  - 2.4 How many spaces are reserved for wheelchairs?
  - 2.5 Which row would be most comfortable for people with long legs?.

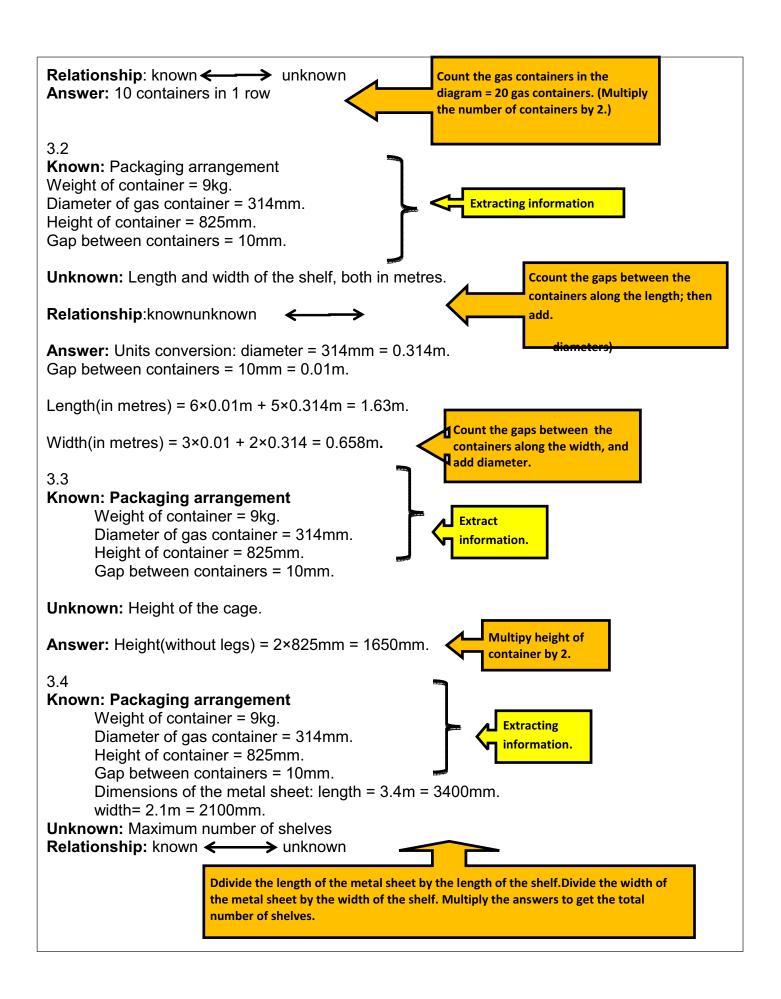
# Shelf Gas bottle Top view of steel cage Empty steel cage Side view of steel cage Empty steel cage Shelf

Diagram5: Packaging arrangement of cylindrical gas containers

- 3.A certified gas dealer sells 9kg gas containers. These cylindrical containers are stored outside the shop in a steel cage, as shown above. There is a gap of 10mm on either side of each gas bottle when they are placed on the shelf in the steel cage.
- 3.1 Calculate the maximum number of gas containers that can fit into ONE steel cage.
- 3.2 Determine the dimensions of the rectangular shelf in metres.
- 3.3 Calculate the weight of the gas containers in a filled cage.
- 3.4 Determine the height of a cage, without its legs.
- 3.5 The company sells rectangular metal sheets with dimensions 3,4 m by 2,1 m. Determine the maximum number of shelves for the steel cage that could be cut from ONE metal sheet. Show ALL calculations.



**Unknown:** The maximum number of gas bottles in a cage.



Number of shelves = 
$$\frac{3400 \text{ mm}}{1630 \text{ mm}}$$
 x  $\frac{2100 \text{ mm}}{658 \text{ mm}}$  = 2 x 3 = 6.

### Activity 3(DBE May/June 2018 P2)

Landy has a contract to deliver 2 750 wooden toy storage boxes without lids. The dimensions of a sheet of plywood and a box are shown below.

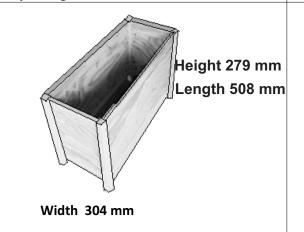
Picture of a sheet of plywood

Woodentoy storage box



**York Timbers Plywood Pine** 

2 440 mm × 1 220 mm × 12 mm



[Source: www.yorktimber.com]

Diagram 6 below shows the layout of the parts of toy storage boxes on ONE sheet of plywood.

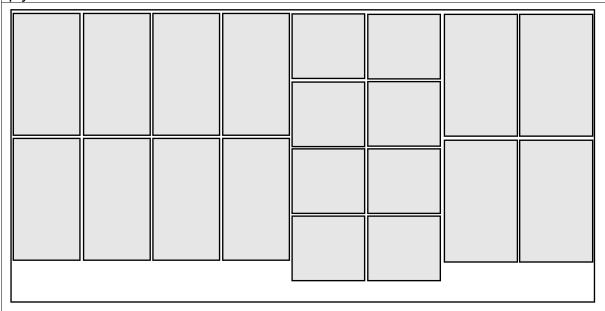


Diagram 6

Use the information above to answer the questions that follow:

- 3.1 Determine how many complete boxes can be cut from ONE sheet of plywood.
- 3.2 Verify whether 687 sheets of plywood will be enough to make 2 750 boxes. Show ALL calculations.

### 6. Check your answers

### **Activity 1**

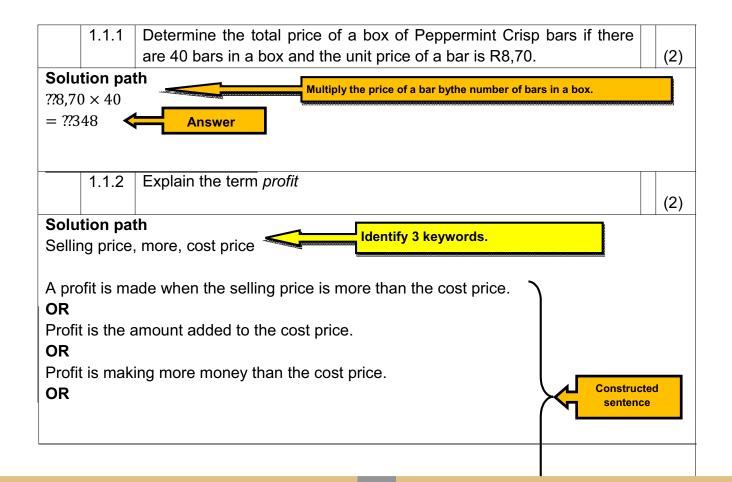
Α

Tyrone buys chocolates in bulk to make gift baskets containing different chocolate bars, which he will sell. He buys boxes that contain bars of Peppermint Crisp, BarOne, Kit Kat, and Cadbury 80g chocolate slabs.

Picture of a gift basket with chocolate bars.



DBE JUNE 2017 P1 Q1



There is a positive difference between income and expenditure. OR Income is more than cost or expenses. OR There is extra money after the sale of the product. 1.1.3 A box of Kit Kat bars costs R435,04. To determine the selling price, Tyrone increases the cost price by 40%. Determine the amount that he adds to the cost price. (2) **Solution Path** Multiply the percentage increase by the price of a box of Kit Kat bars.  $??????????? = 40\% \times ??435,04$ = ??174,016 Calculator answer (as it appears on the calculator). Answer(rands andcents).

В

### **DBE NOV 2017 P1 Q2**

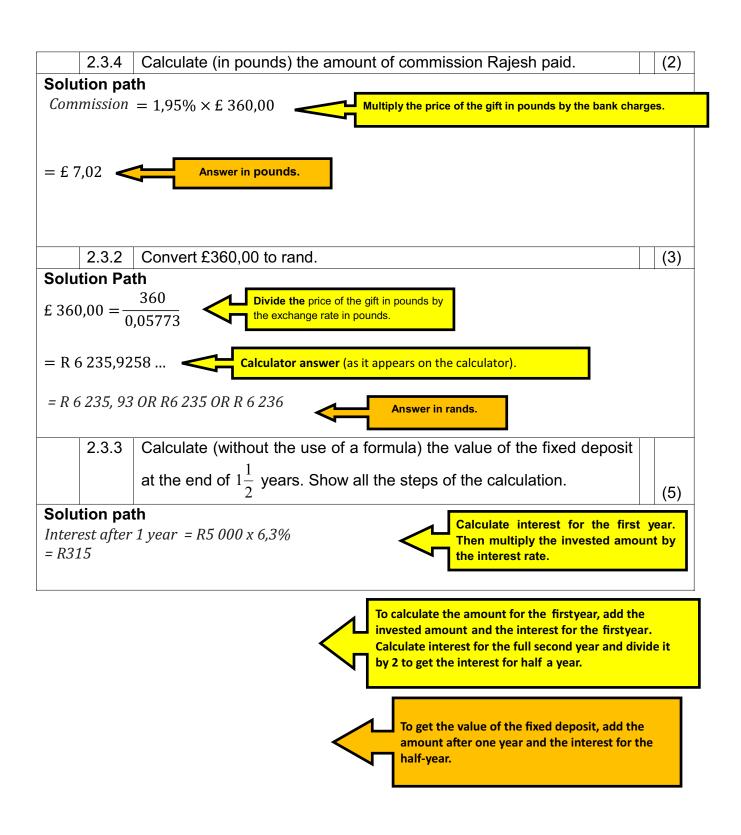
2.3 Rajesh changed a gift of £360,00 into South African rand at a bank.

The exchange rate was R1,00 = £0,05773.

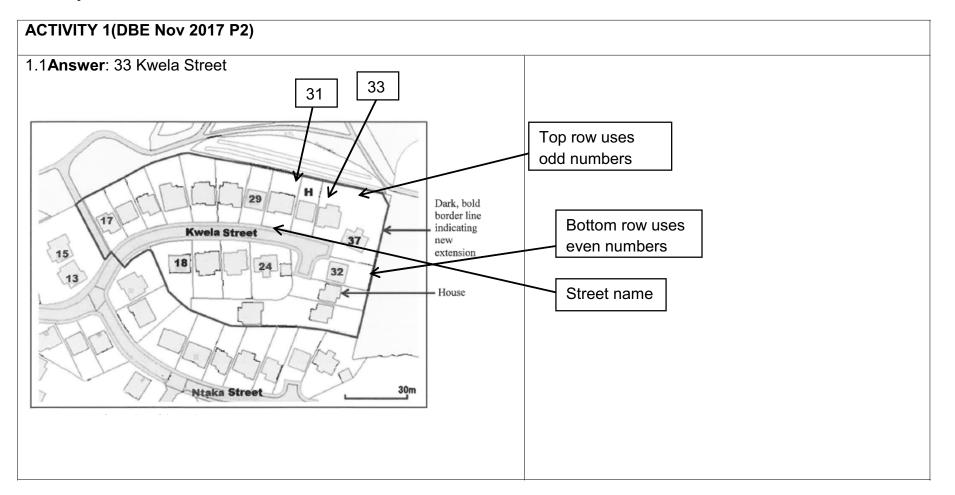
The bank charged 1,95% commission on the amount exchanged.

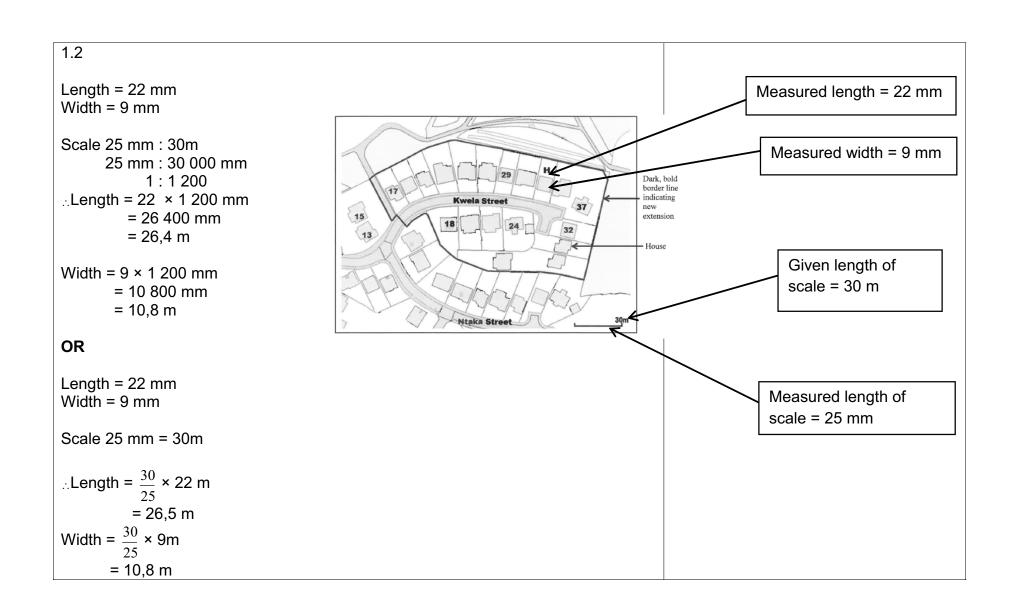
Rajesh then invested R5 000 of his gift in a fixed deposit account for  $1\frac{1}{2}$  years at a compound interest rate of 6,3% per annum.

- 2.3.1 Calculate (in pounds) the amount of commission Rajesh paid. (2)
- 2.3.2 Convert £360,00 to rand. (3)
- 2.3.3 Calculate (without the use of a formula) the value of the fixed deposit at the end of  $1\frac{1}{2}$  years. Show all the steps of the calculation. (5)



### **Check your answers**





### 1.3 On the enlarged map

Measure length = 62 mm

Scaled length = 62 mm 
$$\div$$
 5  
= 12,4 mm  $\neq$  22 mm

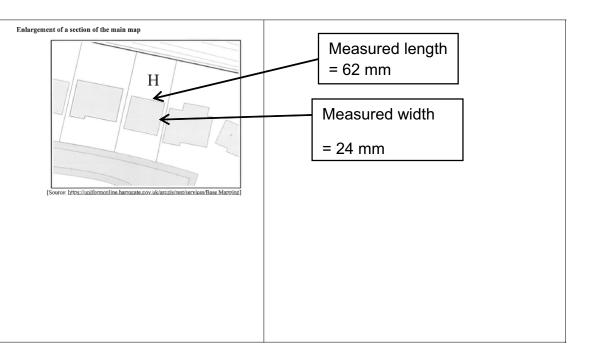
∴ Not valid

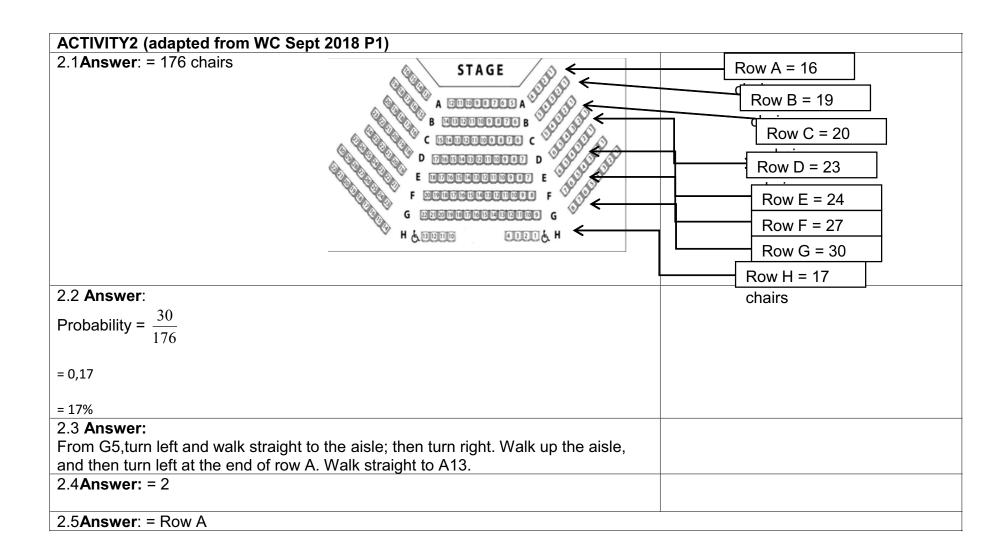
### OR

Measure width = 24 mm

Width = 
$$9 \text{ mm} \times 5$$
  
=  $45 \text{ mm} \neq 24 \text{ mm}$ 

∴ Not valid



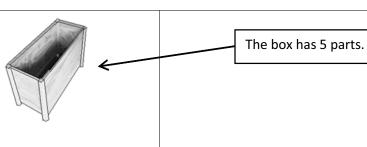


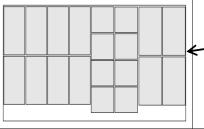
### ACTIVITY 3(DBE May/June 2018 P2)

3.1

Answer: = 
$$\frac{20}{5}$$

= 4 boxes





The layout has 20

3.2Answer:

Number of sheets = 
$$\frac{2750}{4}$$

∴ Not enough

OR

Number of sheets =  $687 \times 4$ 

∴ Not enough

### 7. Message to Grade 12 learners from the writers



### 8. Thank you/ Acknowledgements

A candle does not lose any of its light by lighting another candle. It took a collective to put together this material. That is why two heads will always be better than one. A very big thank you to the provincial colleagues who made themselves available to develop this material. Their names are:

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Together we can!

# MATHEMATICS LITERACY BOOK 2: SOLUTIONS PATHWAYS

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